

1. What is the Bravais lattice formed by all points with cartesian coordinates (l, m, n) if
- [2 Marks] l, m and n are either all odd or all even.
 - [2 Marks] The sum of l, m and n is required to be even.
(Marks will be given only if the reason is provided).

2. [3+1+1 Marks] For a simple hexagonal Bravais lattice with unit vectors:

$$\vec{a}_1 = a\hat{i}, \quad \vec{a}_2 = \frac{a}{2}\hat{i} + \frac{\sqrt{3}a}{2}\hat{j}, \quad \vec{a}_3 = c\hat{k}$$

find the reciprocal lattice and its lattice constants. What is angle between \vec{a}_1 and \vec{b}_1 .

3. It is often convenient to represent fcc Bravais lattice as simple cubic with a cubic primitive cell of side 'a' and a four-point basis.
- [2 Marks] Write the vectors representing the four-point basis.
 - [2 Marks] Show that the structure factor is then either 4 or 0 at all points of the simple cubic reciprocal lattice.
 - [2 Marks] Determine the structure left, when all points with zero structure factors are removed. How the the structure related to fcc?

structure factor: $S_{\vec{k}} = \sum_{j=1}^n \exp(i\vec{k} \cdot \vec{d}_j)$

END