

7. Explain how overtaking sight distance (OSD) is calculated using IRC and AASHTO methods.

(3)

$$\text{OSD} = d_1 + d_2 + d_3 \quad (\text{IRC})$$
$$= v_b t + (2.5 + v_b) T + v T$$

~~T~~ IS:

$$T = \dots$$

AASHTO

$$= d_1 + d_2 + d_3 + d_4$$

Explain??

Some useful formulas

$$P_x = \frac{e^{-\lambda x}}{\sum_{i=0}^{\infty} e^{-\lambda x}}; \quad \min S(x) = \sum_{i=0}^{\infty} x_i f_i(x_i); \quad f_i = 0.01 \left(1 + \frac{V}{44.73}\right); \quad P_{n_0} = (\rho/2) C_x A_i V^3;$$

$$\bar{v}_x = \frac{1}{\frac{1}{n} \sum_{i=1}^n \frac{1}{v_i}}; \quad v_i = \sum v_i/n; \quad q = k; \quad \bar{v}_i; \quad P(n) = (2\lambda)^n \exp(-\lambda t) / n!$$

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Instructions: i) Answer ALL the questions in the space provided. ii) Assume any data required suitably, and iii) Same useful formulas are given at the end

1. The utility function of a logit model of choice between car, carpool and bus are given below, where

A_i/W indicates number of cars per household.

$$V_c = -T_c - 5C_c/W + 0.10A/W; V_{cp} = -T_{cp} - 5C_{cp}/W + 0.05A/W; V_b = -T_b - 5C_b/W$$

Show that if the coefficients b_1 and b_2 have appropriate values (find those values), you obtain the same choice probabilities from logit model whose utility function is:

$$V_c = -T_c - 5C_c/W; V_{cp} = -T_{cp} - 5C_{cp}/W + b_1A/W; V_b = -T_b - 5C_b/W + b_2A/W \quad (3)$$

Utility Car

$$-T_c - 5C_c + \frac{0.10A}{W} \quad \text{Carpool} \quad -T_{cp} - 5C_{cp} + \frac{0.05A}{W}$$

$$-T_c - 5C_c + \frac{0.10A}{W} \quad \text{Bus} \quad -T_b - 5C_b + \frac{b_2A}{W}$$

Pearl = $\frac{e^{-T_c - 5C_c + 0.10A/W}}{e^{-T_c - 5C_c + 0.10A/W} + e^{-T_{cp} - 5C_{cp} + 0.05A/W} + e^{-T_b - 5C_b + b_2A/W}}$

$$e^{-T_c - 5C_c} \left(e^{-\frac{T_c - 5C_c}{W} + \frac{0.1A}{W}} + e^{-\frac{T_{cp} - 5C_{cp}}{W} + \frac{0.05A}{W}} + e^{-\frac{T_b - 5C_b}{W} + \frac{b_2A}{W}} \right)$$

$$= e^{-T_c - 5C_c} \left(e^{-\frac{T_c - 5C_c}{W} + \frac{0.1A}{W}} + e^{-\frac{T_{cp} - 5C_{cp}}{W} + \frac{0.05A}{W}} + e^{-\frac{T_b - 5C_b}{W} + \frac{b_2A}{W}} \right)$$

$$= e^{-T_c - 5C_c} \left(e^{-\frac{T_c - 5C_c}{W} + \frac{0.1A}{W}} + e^{-\frac{T_{cp} - 5C_{cp}}{W} + \frac{0.05A}{W}} + e^{-\frac{T_b - 5C_b}{W} + \frac{b_2A}{W}} \right)$$

$$(b_1 + 1) = 0.05 \quad b_2 + 1 = 0 \quad b_2 = -1$$

$$b_1 = 0.05 - 1 \quad b_2 = -0.05$$

2. Define user equilibrium through Wardrop's first principle? How would you arrive at user optimal flows by mathematical programming method? (2)

Wardrop's 1st principle says that in congested road the used road have equal B4 minimum travel cost and used road have greater cost. User optimal flows = $\frac{2}{1+1}$

$$\frac{ds}{dx}$$

3. Two routes connect an origin-destination pair with performance functions, $t_1 = 5 + 3x_1$ and $t_2 = 7 + x_2$ with the x 's expressed in thousands of vehicles per hour and t 's expressed in minutes. The origin-destination demand is 7000 veh in peak hour. What is the value of the derivative of the user equilibrium math program evaluated at the system-optimal solution with respect to x_1 (x_1 equal to system-optimal solution) t_1 (veh/h)

Nodes 2
 $t_2 = 7 + x_2$ veh/h

$q = 7$ veh/h

$x_1 + x_2 = 7$
 system at x_1 obtained from system optimal

$\Rightarrow x_1 t_1 + x_2 t_2$
 $x_1(5 + 3x_1) + x_2(7 + x_2)$

$x_2 = 7 - x_1$

$\Rightarrow 5x_1 + 3x_1^2 + (7 - x_1)(7 + x_1)$

$5x_1 + 3x_1^2 + (7 - x_1)(14 - x_1)$

$5x_1^2 + 3x_1^2 + 98 - 7x_1 - 14x_1 + x_1^2$

$\Rightarrow 9x_1^2 - 21x_1 + 98$
 $\frac{ds(x)}{dx_1} = 0 \Rightarrow 18x_1 - 21 = 0 \Rightarrow x_1 = \frac{21}{18} = \frac{7}{6} = 1.167$ veh/h

$S(x) = 4x_1^2 - 16x_1 + 98$

$\frac{dS(x)}{dx_1} = 0 \Rightarrow 8x_1 - 16 = 0 \Rightarrow x_1 = \frac{16}{8} = 2$ veh/h

now

4. Assume that you are standing adjacent to a six-lane divided highway (three lanes in each direction). Lane 1 has vehicles traveling at 50 km/h, and lane 2 vehicles at 75 km/h, and lane 3 vehicles at 100 km/h. The spacing between vehicles on each of the lane is 150 m, and your observation period is 30 minutes. What is the time mean speed of the traffic stream?

Lane 1	Lane 2	Lane 3
50 km/h	75 km/h	100 km/h

$l = 6 \times 150 \text{ m} = 900 \text{ m}$
 $m_1 = 50 \text{ km/h} = 27.78$
 $m_2 = 41.67$
 $m_3 = 55$

A vehicle manufacturer is considering an engine for a new sedan to be launched ($C_D = 0.30$, $A_f = 2.0$ m²). The car will be tested at a maximum speed of 160 km/h on a paved surface at sea level ($\rho = 1.2256$ kg/m³). The car currently weighs 9.3 kN, but the designer selected an underpowered engine because aerodynamic and rolling resistance were ignored. If 9N of additional vehicle weight is added for each kW of power needed to overcome the neglected resistance, what will be the final weight of car if it is to achieve the 160 km/h top speed? (3)

$$\frac{160 \text{ km}}{\text{hr}} \times \frac{5}{18} = 44.44 \text{ km/s}$$

$$P_{\text{max}} = (R_a + R_{rl}) V_{\text{max}}$$

$$R_a = \frac{1}{2} \rho C_D A_f V_{\text{max}}^2 = \frac{1.2256 \times 0.30 \times 7 \times (44.44)^2}{2} = 726.136 \text{ N} = 0.726 \text{ kN}$$

$$f_{rl} = 0.01 \left(1 + \frac{V}{44.73} \right) = 0.01 \left(1 + \frac{44.44}{44.73} \right) = 0.02$$

$$R_{rl} = f_{rl} \times W = 0.02 \times 9.3 = 0.186 \text{ kN}$$

$$P_{\text{max}} = (0.726 + 0.186) \times 44.44 = 40.529 \text{ kW}$$

$$1 \text{ kW} \rightarrow 9 \text{ N} \rightarrow 9 \times 10^{-3} \text{ kN} \rightarrow 0.009 \text{ kN}$$

$$40.529 \text{ kW} \rightarrow 40.529 \times 9 \times 10^{-3} = 0.365 \text{ kN}$$

No final weight = 9.3 + 0.365

$$= 9.665 \text{ kN}$$

5. An observer counts 360 veh/h at a specific highway location. Assuming that the arrival of vehicles at this location is Poisson distributed, estimate the probability of having 4 or more vehicles arriving over a 20-second interval. (3)

$$q = 360 \text{ veh/hr} \rightarrow \lambda = 360 \left(\frac{20}{3600} \right) = 2$$

20
40