

ELL786: Multimedia Systems

Minor 1 Examination, Duration: 1hr

Note: All questions are compulsory.

Q1.

- a. With the help of a block diagram clearly describe the working of the encoder in a predictive coding scheme. Clearly label all the blocks and explain their function.
- b. A source outputs a sequence of symbols whose autocorrelation sequence can be represented as

$$R_x(0) = 26, R_x(1) = 7, R_x(2) = 7/2$$

Obtain the coefficients of a 2nd order predictive coder to encode any sequence that this source generates.

- c. Derive the expression of prediction error. What is the prediction error in the example given above? (3+4+3)

Q2. Consider the following 4, 2D points:

$$\begin{pmatrix} 2 \\ 1 \end{pmatrix} \\ \begin{pmatrix} 3 \\ 2 \end{pmatrix} \begin{pmatrix} 3 \\ 2 \end{pmatrix} \begin{pmatrix} 4 \\ 3 \end{pmatrix} \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

- a. Obtain the eigen vectors and eigen values and apply KL transform.
- b. Plot the points before and after the transform and comment on the result. (8+2)

Q3. Given a memory-less source with alphabet {a, b, c, d}, the probabilities of occurrence of the 4 symbols are 0.5, 0.3, 0.15, 0.05 respectively.

- a. What is the entropy of this source?
- b. Apply **Huffman coding** and obtain the bits/symbol value for the code.
- c. Given the sequence 'cddb', obtain the code corresponding to this sequence if **arithmetic coding** is applied.
- d. Construct Golomb code to represent symbols of this source. What is the value of the parameter *m* chosen? Justify the choice. Obtain the bit/symbol value for the code. (1+3+4+4)

Q4. Assume another memory-less source with alphabet {a, b, c} and probabilities of occurrence 0.4, 0.3, 0.3 respectively.

- a. Construct a minimum variance Huffman code for the case where two symbols are concatenated to construct the extended alphabet. Compare the bits/symbol value with the Entropy of the source.
- b. Show mathematically that extending the symbols can help construct a code whose bits/symbol value approaches the Entropy of the source. (5+3)

Handwritten notes:
 $d(n) = x_n - \hat{x}(n)$
 $\hat{x} = a_1 x_{n-1} + a_2 x_{n-2} + \dots + a_m x_{n-m}$
 $\hat{x}_1 = 2.179$
 $\hat{x}_2 = 3.52$
 $\hat{x}_3 = 2.179$
 $\hat{x}_4 = 3.52$

Handwritten numbers:
 0.442
 0.376
 0.127