

**Department Of Mathematics  
Indian Institute Of Technology, Delhi  
MINOR – II TEST**

Time 1 Hour

MAL 382 – Theory of Automata

Full Marks - 21

Date: March 25, 2014

- Q1. a) Design a PDA that accepts the language  $\{a^n b^m \mid 1 < n < m\}$  by Final State  
 b) Design a PDA that accepts the language  $\{a^n b^m \mid n > m > 1\}$  by Empty Stack

For both the problems explain your algorithm clearly before describing the PDA.

[4 + 3 = 7]

- Q2. a) Write the grammar to accept Arithmetic expressions given as below:

- An identifier is an Arithmetic expression - where an identifier is of maximum 2 characters from  $\Sigma = \{a, b\}$
- Given an arithmetic expression E, (E) is an arithmetic expression
- Given two arithmetic expressions A and B,  $A + B$  and  $A - B$  are arithmetic expressions.

- b) Express the above grammar in CNF.

[2 + 5 = 7]

- Q3. a) Explain the CYK algorithm. What is its complexity? Justify your answer.

- b) Consider the grammar G with the following production rules:

$S \rightarrow AB$   
 $A \rightarrow a$   
 $B \rightarrow b \mid CD$   
 $C \rightarrow AB$   
 $D \rightarrow c$

Use CYK algorithm to check whether the string "aaabccc" belongs to  $L(G)$ .

[3 + 4 = 7]

$AB$   
 $\leftarrow CD$   
 $aABc$   
 $aaCcc$   
 $a \rightarrow ABcc$   
 $aaabcc$

$AB$   
 $AABcc$

$S \rightarrow aB$