



Total marks 15

Time: 60 min

1 Consider two spins, defined by the spin angular momenta  $S_1$  and  $S_2$ , undergo some interaction given by an interaction strength  $A$ . What would be the resulting ground state of the coupled system if  $A > 0$ ? Assume that the eigenvalue of  $S^2 = 3/4$ . [2.5]

2. a) Consider a ferromagnet introduced to an external magnetic field  $H_{ext}$ . Show that the  $\vec{\nabla} \cdot H_{ext}$  is non zero [1]

b) Show that the internal magnetic field within the ferromagnetic material is different from  $H_{ext}$  [1.5]

c) If the susceptibility is measured as the induced magnetization due to external field, show that the ratio of measured susceptibility (experimental) and internal susceptibility is given by

$$\frac{\chi_{experimental}}{\chi_{internal}} = \frac{1}{1 + N \cdot \chi_{internal}}$$

where,  $N$  is the demagnetization factor [2]

d) If the magnet is cooled down from above the Curie temperature  $T_c$ , show that the measured susceptibility (in a very small field) is the inverse of the demagnetization factor. [1.5]

3 a) Consider a compound containing octahedrally coordinated  $Fe^{2+}$ . Write down the total spin angular momentum ( $S$ ) for low spin and high spin state at zero temperature. Atomic no. of Fe is 26. [3.5]

b) If the low spin energy level lies just 50 meV below the high-spin level, at what temperature would you expect spin crossover from low spin state to high-spin state to occur? [1.5]

4. a) Discuss the role of orbital quenching in defining the magnetic ground state of 3d ions. [2]

b) For a ferromagnet, it can be shown that  $3k_B T_c = g\mu_B(J+1)AM_s$ . Estimate the Weiss molecular field for Gd ( $T_c = 292$  K,  $J=S=7/2$ ). [1.5]

5. In a cubic crystal, the magnetocrystalline anisotropy energy is given by

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$$E = K_1(\alpha_1^2 \alpha_2^2 + \alpha_2^2 \alpha_3^2 + \alpha_1^2 \alpha_3^2) + K_2 \alpha_1^2 \alpha_2^2 \alpha_3^2 + \dots$$

where  $K$ 's are anisotropy constants and  $\alpha$ 's are the direction cosines. Estimate the value for  $E$  for  $[100]$  and  $[111]$  directions. [3]

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$$\hbar = 1.054 \times 10^{-34} \text{ Js}, k_B = 1.38 \times 10^{-23} \text{ J/K}, \mu_B = 9.274 \times 10^{-24} \text{ J/T}, \mu_0 = 4\pi \times 10^{-7} \text{ Tm/A}$$

Note: All notations used in the questions have their usual meanings.

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3  
1